## M.Com.

## MATHEMATICS

# 402-B : Operations Research (CBCS 2019 Pattern) (Semester-IV) 

Time : 3 Hours]
[Max. Marks : 60
Instructions to the candidates:

1) Question No. 1 and question No. 6 are compulsory.
2) Solve any three questions from questions No. 2 to questions No. 5
3) Figures to the right side indicates full marks.

Q1) Fill in the blanks by selecting suitable choice (any 6 out of 8 ).
a) In game theory, the outcome or consequence of a strategy is referred as the $\qquad$
i) Penalty
ii) Pay off
iii) Reward
iv) end-game strategy
b) A mixed strategy game can be solved by $\qquad$
i) Simplex method
ii) Hungarian method
iii) Graphical method
iv) Degeneracy
c) For a maximization problem, objective function coefficient for an artificial variable is $\qquad$
i) +M
ii) 0
iii) -1
iv) -M
d) A set of feasible solution to a linear programming problem is $\qquad$
i) Polygon
ii) triangle
iii) bold
iv) convex
e) To find initial basic feasible solution of a T.P. the method which starts allocations from the lowest cost is called $\qquad$ method.
i) north west corner
ii) South east corner
iii) least cost
iv) Vogel's approximation
f) In a T.P the method of penalties is called $\qquad$
i) least cost
ii) vogel's approximation
iii) north east corner rule
iv) Hungarian method
g) $\qquad$ is an event oriented network diagram.
i) PERT
ii) Histogram
iii) CPM
iv) Ogive
h) An activity which doesnot consume either resource or time is called $\qquad$
i) Predecessor activity
ii) Successor activity
iii) Terminal activity
iv) Dummy activity

Q2) Attempt any two of the following.
a) Find IBFS of the following transportation problem using North west corner method Also find the transportation cost.

|  | A | B | C | D |  | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P | 2 | 11 | 10 | 3 | 7 | 4 |
| Q | 1 | 4 | 7 | -2 | 1 | 8 |
| R | 3 | 9 | 4 | ] 8 | 12 | 9 |
| Demand | 3 | 3 | $4$ | 5 | 6 |  |

b) Solve the following L.P.P. by graphical method

Minimize $\quad Z=40 x_{1}+36 x_{2}$
Subject to $\quad x_{1} \leq 8$

$$
x_{2} \leq 10
$$

$$
5 x_{1}+3 x_{2} \geq 45
$$

$$
x_{1}, x_{2} \geq 0
$$

c) Explain rules of dominance in game theory.

Q3) Attempt any two of the following.
a) Write the dual of the following L.P.P.

Maximize $\quad(Z)=5 x_{1}+7 x_{2}$
Subject to $\quad x_{1}+x_{2} \leq 4$

$$
\begin{aligned}
& 3 x_{1}+8 x_{2} \leq 24 \\
& 10 x_{1}+7 x_{2} \leq 35 \\
& x_{1}, x_{2} \geq 0
\end{aligned}
$$

b) Obtain IBFS of the following T.P. using matrix minima method. Also find the transportation cost.

| Destination |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |

c) Find minimum cost spanning tree for the following network.


Q4) Attempt any two of the following.
a) Solve the following assignment problem to minimize the total cost.

|  | a | b | d $\mathrm{d}^{\text {d }}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| I | 160 | 130 | 190 | 200 |
| II | 135 | 120 | 160 | 175 |
| III | 140 | 110 | 170 | 185 |
| IV |  |  | 80 | 110 |
| V | 55 | 35 | 80 | 105 |

b) Define network. Explain what do you mean by directed and undirected network? Also explain the terms Node and Arc.
c) Determine the saddle point and optimal strategies for each player'. Also find value of the game.

## Player B

$$
\left.\begin{array}{cc} 
& \\
& \text { I } \\
\text { Player A } & \text { II }
\end{array} \begin{array}{ccc}
\text { I } & \text { II } & \text { III } \\
-4 & -3 & 0 \\
3 & 0 & 3 \\
6 & -3 & 4
\end{array}\right]
$$

Q5) Attempt any two of the following.
a) Discuss the various steps involved in the application of PERT and CPM.
b) Solve the following L.P.P. by simplex method

Minimize $\quad(Z)=x_{1}-3 x_{2}+2 x_{3}$
Subject to $\quad 3 x_{1}-x_{2}+3 x_{3} \leq 7$
$-2 x_{1}+4 x_{2} \leq 12$
$4 x_{1}+3 x_{2}+8 x_{3} \leq 10$
$x_{1}, x_{2}, x_{3} \geq 0$
c) Solve the following assignment problem for maximization.
A
P
$\mathrm{P}\left[\begin{array}{ccc}\mathrm{B} & \mathrm{C} & \mathrm{D} \\ \mathrm{Q} \\ \mathrm{R} & 35 & 28\end{array}\right.$
R
S $\left[\begin{array}{cccc}21 \\ 30 & 25 & 20 & 15 \\ 30 & 25 & 20 & 15 \\ 24 & 20 & 16 & 12\end{array}\right]$

Q6) Attempt any two of the following
a) Draw the graph and highlight the feasible region for the given constraints

$$
x_{1}+x_{2} \leq 2 \text { and } 2 x_{1}+x_{2} \geq 3
$$

b) Write canonical form of the following LPP.

Maximize $\quad(Z)=15 x_{1}+x_{2}$
Subject to $x_{1}+2 x_{2} \leq 10$

$$
2 x_{1}+3 x_{2}=12
$$

$$
x_{1}+x_{2} \geq 3
$$

$$
x_{1}, x_{2} \geq 0
$$

c) Explain the following terms with reference to transportation problem
i) Balanced T.P.
ii) I.B.F.S.
iii) Optimal Solution
d) i) Explain Minimum cost capacitated network
ii) Give model difinition of Max-min networks.

