## M.Com.

422B/402 : OPERATIONS RESEARCH (2019 Credit Pattern) (Semester - IV) (CBCS)

## Time : 3 Hours]

[Max. Marks : 60
Instructions to the candidates:

1) Question No. 1 and Question No. 6 are compulsory.
2) Solve any three questions from question No. 2 to question No. 5.
3) Figures to the right side indicates full marks.

Q1) Fill in the blanks by selecting suitable choice (any 6) :
a) A game is said to be strictly determinable if
i) Maximin value $=$ minimax value
ii) Maximin value $\leq$ minimax value
iii) Maximin value $\geq$ minimax value
iv) Maximin value $\neq$ minimax value
b) Linear Programming method should be used to determine value of the game when size of payoff matrix is $\qquad$
i) $3 \times 4$
ii) $2 \times 2$
iii) $m \times 2$
iv) $2 \times n$
c) Key element is also known as $\qquad$

1) Slack
ii) Surplus
iii) Artificial
iv) Pivot
d) If the given Linear programming Problem is in its standard form then primal-dual pair is $\qquad$
i) Square
ii) Triangle
iii) Un-symmetric
iv) Symmetric
e) $\qquad$ or $\qquad$ are used to "Balance" an assignment or transportation problem.
i) Destination, sources
ii) Dummy rows, dummy columns
iii) Units supplied, units demanded iv) Artificial cells, degenerate cells
f) When a maximization assignment problem is converted in minimization problem, the resulting matrix is called $\qquad$ .
i) Cost matrix
ii) Profit matrix
iii) Regret matrix
iv) Dummy matrix
g) The difference between total and free float is $\qquad$
i) Total
ii) Initial activity
iii) Independent
iv) Interference
h) Activities lying on critical path are called $\qquad$
i) Dummy activities
ii) Critical activities
iii) Non-critical activities
iv) Initial activities

Q2) Attempt any two of the following:
a) Solve the following LPP by

Graphical method
Maximize $\mathrm{z}=50 x_{1}+40 x_{2}$
Subject to, $\quad 6 x_{1}+4 x_{2} \leq 24$

$$
x_{1}+2 x_{2} \leq 6
$$

$$
-x_{1}+x_{2} \leq 1
$$

$$
x_{1} \leq 2
$$

$x_{1}, x_{2} \geq 0$
b) Find an initial basic feasible solution of the following transportation problem using North-West corner method.

| Destination | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Supply |
| :---: | :---: | :---: | :---: | :---: |
| Origin |  |  |  |  |
| $\mathrm{O}_{1}$ | 13 | 15 | 16 | 17 |
| $\mathrm{O}_{2}$ | 7 | 11 | 2 | 12 |
| $\mathrm{O}_{3}$ | 19 | 20 | 9 | 16 |
| Demand | 14 | 8 | 23 |  |

Also find the transportation cost.
c) Define the following terms :
i) Pure strategy
ii) Pay off
iii) Fair game

Q3) Attempt any two of the following :
a) Find the minimum cost spanning tree for the following network.

b) Solve the following assignment problem for minimization.

|  |
| :--- |
| A |
| A |
| B |
| C |
| D |\(\quad\left[\begin{array}{ccccc}25 \& 18 \& 32 \& 20 \& 21 <br>

34 \& 25 \& 21 \& 12 \& 17 <br>
20 \& 17 \& 20 \& 32 \& 16 <br>
20 \& 28 \& 20 \& 16 \& 17\end{array}\right]\)
c) Write canonical form of the following LPP.

Maximize $\quad z=15 x_{1}+3 x_{2}$
Subject to, $\quad x_{1}+2 x_{2} \leq 10$
$2 x_{1}+3 x_{2}=14$
$x_{1}+x_{2} \geq 3$
$x_{1}, x_{2} \geq 0$
Q4) Attempt any two of the following :
a) Solve the following $2 \times 2$ game by algebraic method.

Player B

Player A

| I | II |
| :---: | :---: |
| 2 | -1 |
| -1 | 0 |

b) Discuss the various steps involved in the application of PERT and CPM.
c) The following is a solution of a transportation problem.

| (20) 1 | 2 | (10) 1 | 4 |
| :---: | :---: | :---: | :---: |
| 3 | (20) 3 | (20) 2 | (10) 1 |
| 4 | (20) 2 | 5 | 9 |

Show that it is an optimal solution and find an alternate optimal solution, if it exists.

Q5) Attempt any two of the following:
a) Define the following terms :
i) Loop
ii) Forward pass
iii) Backward pass
b) Solve the following LPP by simplex method

Maximize $\quad \mathrm{z}=x+4 y$
Subject to, $\quad x+2 y \leq 2$
$4 x+3 y \geq 12$
$x, y \geq 0$
c) Solve the following assignment problem for maximization.

|  | A | B | C | D |
| :---: | :---: | :---: | :---: | :---: |
| I | $\left.\begin{array}{cccc}100 & 140 & 280 & 70 \\ \text { II } & 130 & 160 & 200 \\ 60 \\ \text { III } & 80 & 130 & 300 \\ 90 \\ \text { IV } & 150 & 110 & 250 \\ \hline\end{array}\right)$. |  |  |  |

Q6) Attempt any two of the following
a) Define the following terms:
i) Objective function
ii) Optimum solution
b) Draw the graph and highlight the feasible region for the constraints given below:

$$
\begin{aligned}
& x+2 y \geq 6 \\
& 3 x+y \geq 9 \\
& x+y=7 \\
& x, y \geq 0
\end{aligned}
$$

c) Write the dual of the following LPP.

Minimize $\quad \mathrm{z}=10 x_{1}+8 x_{2}$
Subject to, $\quad x_{1}+2 x_{2} \geq 5$
$2 x_{1}-x_{2} \geq 12$
$x_{1}+3 x_{2} \geq 4$
$x_{1} \geq 0, x_{2}$ is unrestricted
d) Explain the following terms :
i) Critical event
ii) Earliest finish time

