

Total No. of Questions : 6]

SEAT No. :

P507

[Total No. of Pages : 2

APR - 18/TE/Insem. - 106

T.E. (Mechanical / Automobile)

NUMERICAL METHODS AND OPTIMIZATION

(2015 Course) (Semester - II) (302047)

Time : 1 Hour]

[Max. Marks : 30

Instructions to the candidates:

- 1) *Solve Q1 or Q2, Q3 or Q4, Q5 or Q6.*
- 2) *Neat diagrams must be drawn wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Use of programmable calculator is not permitted.*
- 5) *Assume suitable data, if necessary.*

Q1) a) In a cam follower system the displacement 'd' of the follower tip in term of angle of rotation ' θ ' is given by **[6]**

$$d = \theta + \sin(\theta) \quad 0 \leq \theta \leq 2\pi .$$

Determine value of ' θ ' which produces displacement $d = 1$ cm. Check convergence and solve upto 4 decimal place accuracy. Take initial guess 0.

- b) Define the following terms: **[4]**
- i) Error propagation.
 - ii) Significant digits.
 - iii) Relative error.
 - iv) Truncation error.

OR

Q2) a) Draw the flowchart for Bisection method. **[6]**

- b) Round off the number 8.74350 to three significant digits and compute relative error, absolute error and percentage error. **[4]**

Q3) Solve by Gauss Seidal method for four decimal accuracy for the following system of equations : **[10]**

$$28x + 4y - z = 32$$

$$x + 3y + 10z = 24$$

$$2x + 17y + 4z = 35$$

OR

P.T.O.

Q4) a) Solve the following equations with Thomas algorithm. [6]

$$x_1 + 2x_2 = 4$$

$$-x_1 + x_2 + 2x_3 = 1$$

$$x_2 + 3x_3 + x_4 = 7$$

$$2x_3 + 2x_4 = 8$$

b) Explain step by step procedure for Gauss Jacobi method to compute solution of simultaneous equations. Comment on convergence of Gauss Jacobi method and Gauss Seidal method. [4]

Q5) Minimize $Z = 600x_1 + 500x_2$ [10]

Subjected to condition

$$2x_1 + x_2 \geq 80$$

$$x_1 + 2x_2 \geq 60$$

$$x_1, x_2 \geq 0$$

Use Simplex method.

OR

Q6) a) Maximize $Z = x + (y/2)$ [6]

Subjected to condition

$$3x + 2y \leq 12$$

$$5x \leq 10$$

$$x + y \leq 18$$

$$-x + y \geq 4$$

$$x, y \geq 0$$

Solve by graphical method.

b) Define the following terms : [4]

i) Feasible solution.

ii) Non negativity condition.

iii) Constraints.

iv) Optimal solution.

