

Total No. of Questions : 6]

SEAT No. :

**P544**

[Total No. of Pages : 2

**APR - 18/TE/Insem. - 147**

**T.E. (Information Technology)**

**DESIGN AND ANALYSIS OF ALGORITHMS**

**(2015 Course) (Semester - II)**

*Time : 1 Hour]*

*[Max. Marks : 30*

*Instructions to the candidates:*

- 1) *Solve Q1 or Q2, Q3 or Q4, Q5 or Q6.*
- 2) *Neat diagrams must be drawn wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Assume suitable data, if necessary.*

**Q1) a)** Reorder the following complexities from the smallest to the largest [5]

1)  $n \log_2 n$ ,  $n + n^2 + n^3$ , 24,  $\sqrt{n}$ .

2)  $n!$ ,  $2^n$ ,  $(n + 1)!$ ,  $2^{2n}$ ,  $n^n$ ,  $n^{\log n}$

b) Prove by contradiction that square root of 2 is irrational. [5]

OR

**Q2) a)** Explain the potential method of amortized analysis with example. [5]

b) Solve the following recurrence relation using substitution method  
 $T(n) = T(n - 1) + 1$ ,  $T(0) = 0$ . [5]

**Q3) a)** Solve the following instance of job sequencing problem using greedy approach. Let  $n = 6$ , profit  $(1 : 6) = (30, 20, 15, 10, 5, 1)$  and deadlines  $d(1 : 6) = (4, 2, 2, 1, 4, 3)$ . [5]

b) Write a recurrence relation for Merge sort and Find a time complexity using by Master's theorem. [5]

OR

**Q4) a)** Write an algorithm to find Minimum Spanning Tree using Kruskal algorithm and analyze it. [5]

b) Show the steps in multiplying the following two integers using efficiency integer multiplication 2345 and 678. [5]

*P.T.O.*

**Q5) a)** Let  $n = 3$  and  $(a_1, a_2, a_3) = \{\text{do, if, while}\}$ . Let  $P(1 : 3) = \{0.5, 0.1, 0.05\}$  and  $q(0 : 3) = \{0.15, 0.1, 0.05, 0.05\}$ . Compute and construct OBST for above value using dynamic Programming. [8]

b) State and explain the principle of Optimality. [2]

OR

**Q6) a)** Solve the knapsack problem using Dynamic programming for no. of objects  $n = 4$ , given capacity  $M = 8$  [5]

Items	1	2	3	4
Value	15	10	9	5
Weight	1	5	3	4

b) Write a Bellman Ford algorithm to find shortest path and Analyze it. [5]

