| Total N | lo. o | f Que | estions: 9] | ^ | SEAT N | 0.: | \neg | |
|--|-------|--------|--|---------------------|------------------|-------------------|--------|--|
| DD 4062 | | | | 23 | | otal No. of Pages | : 4 | |
| PD-4062 | | | [640 | 2]-21 | <u>.</u> | , | | |
| 9 | S.E | . (E | ٥ | 3 | Comp. Eng. | /Electronics | | |
| S.E. (Electronics /E&TC/Electronics & Comp. Eng./Electronics Engg.(VLSI Design & Tech.)/Electronics & Comm.(A.C.T.)) | | | | | | | | |
| ENGINEERING MATHEMATICS - III | | | | | | | | |
| (2019 Pattern) (Semester - III) (207005) | | | | | | | | |
| Time : | 2½. | | | icstei - | 111) (2070 | [Max. Marks: | 70 | |
| Instructions to the candidates: | | | | | | | | |
| 1 |) | Q.1 | s compulsory. | | | \wedge | | |
| 2 |) | Atter | upt Q.2 or Q.3, Q.4 or Q.5, | Q.6 or Q .7, | Q.8 or Q.9. | <i>?</i> ` | | |
| 3 |) | Neat | diagrams must be drawn v | vherever n | ecessary. | * | | |
| 4 | !) | Figu | res to the right indicate ful | l marks. | | | | |
| 5 | | - \X | of electronic pocket calcula | | wed. | | | |
| 6 | | | me suitable data, if necesso | | 9. | | | |
| 7 |) > | Write | e numerical calculations co | rrect upto | four decimal | places. | | |
| | | | | 3 | 3' | | | |
| <i>Q1</i>) V | Vrite | e the | correct option for the following | owing mu | ltiple choice of | luestions. | | |
| i) |) | Ifφ | $= x^2 - y^2 + 2z^2 \text{ then } \nabla \phi \text{ at}$ | the point | (1, 2, 3) is | ı | [2] | |
| , | | | | (D) | | | / | |
| | | a) | 2i-4j-12k | y b) | 2i - 4j + 12k | | 3 | |
| | | c) | 2i + 4j + 12k | d) | 2i + 4j - 12k | | 50 | |
| 11 | i) | If f() | $f(x) = x^2$, $h = 2$ then $\Delta^2 f(x)$ is | given by | | | [2] | |
| | 4 | a) | 6 | b) | 12 | 1,000 | | |
| 4 | | c) | 4 | d) | 8 | | | |
| ij | ii) | If f | $2i - 4j - 12k$ $2i + 4j + 12k$ $2i + 4j + 12k$ $3i + 4j + 12k$ 4 $(z) = \frac{\sin \pi z^2 + \cos \pi z^2}{(z - 1)^2 (z - 2)} \text{ the } 0$ 1 | en residue | of f(z) at z= | 2 is [| [2] | |
| ~ | | a) | 0 | b) | -1 | | | |
| 1 | | c) | 1 | d) | W | | | |

P.T.O.

| iv) | The work done in moving a particle in a force field $\overline{E} = (2x + y)\overline{i} + (2x + y)\overline{i}$ along the auty $x = 2t$, $y = 2t$ from $t = 0$ to |
|---------------|---|
| | $\overline{F} = (2x+y)\overline{i} + (3y-x)\overline{j}$ along the curve $x = 3t$, $y = 2t$ from $t = 0$ to $t = 1$, is |
| | a) 15 b) 12 |
| | c) 14 d) 0 |
| v) | Shifting operator E is equivalent to [1] |
| | a) $1-\delta$ b) $1+\Delta$ |
| | c) $1 \pm \delta^2$ d) $2 - \delta$ |
| vi) | If f(z) is analytic on and within a closed contour C and if 'a' is any point |
| | If $f(z)$ is analytic on and within a closed contour C and if 'a' is any point within C then by Cauchy's integral formula $\oint \frac{f(z)}{z-a} dz$ is [1] |
| | a) 0 b) $2\pi i f(a)$ |
| | ·P |
| | $\frac{2\pi i}{n!}f^n(a) \qquad \qquad d) \pi i$ |
| \ | |
| a) | State Lagrange's interpolation formula. Use this formula to find y when |
| a) | x = 5 from the following data. [5] |
| | x 2 3 4 7 |
| | y 4 8 16 128 5 |
| b) | A curve is drawn to pass through the points given by the following table. |
| Γ | [5] |
| | x 1 1.5 2 2.5 3 3.5 4 y 2 2.4 2.7 2.8 3 2.6 2.1 |
| | y 2 2.4 2.7 2.8 3 2.6 2.1 Estimate the area bounded by the curve, the X-axis and the ordinates |
| | |
| | $x = 1$, $x = 4$ by Simpson's $\frac{1}{3}$ rule. |
| c) | Use Euler's method to solve [5] |
| | $\frac{dy}{dx} = 1 + xy, \ y(0) = 1$ |
| | and tabulate y for $x = 0$ to $x = 0.3$. Take $h = 0.1$ |
| | 9.7 |
| 2]-2 1 | 2 |

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Q2)

- Q3) a) Given $\sin 45^\circ = 0.7071$, $\sin 50^\circ = 0.7660$, $\sin 55^\circ = 0.8192$, $\sin 60^\circ = 0.8660$, Find $\sin 58^\circ$ using Newton's backward difference formula. [5]
 - b) Given $\frac{dy}{dx} = x^2 y$, y(0) = 1, find y(0.1) using Runge-Kutta method of fourth order (Take h = 0.1) [5]
 - c) Use Trapezoidal rule to evaluate $I = \int_{-3}^{3} x^4 dx$ using six equal subintervals. [5]
- Q4) a) Find the directional derivative of $\phi = xy + yz + zx$ at (1, 1, 1) along the vector $\overline{i} + 2\overline{j} + 2\overline{k}$ [5]
 - b) Show that the vector field $\vec{F} = (6xy + z^3)\vec{i} + (3x^2 z)\vec{j} + (3xz^2 v)\vec{k}$ is irrotational. Find scalar potential function ϕ such that $\vec{F} = \nabla \phi$ [5]
 - Find angle between tangents to the curve x = t, $y = t^2$, $z = t^3$ at t = 1 and t = -1.

Q5) a) Find the directional derivative of $\phi = xyz$ at (1, 2, -1) in the direction normal to the surface $x \log z - y^2 = -4$ at (-1, 2, 1)

- b) Prove that $\nabla^2 \left[\nabla \cdot \frac{\overline{r}}{r^2} \right] = \frac{2}{r^4}$ [5]
- c) The position vector of a particle at time t is $\overline{r} = \cos(t-1)\overline{i} \sin h(t-1)\overline{j} + mt^3\overline{k}$. Find the condition on m. So that at any time t = 1 the acceleration is normal to the position vector. [5]
- **Q6**) a) Apply Green's Theorem to evaluate $\int_C (3ydx + 2xdy)$ where C is boundary of $0 \le x \le \pi$, $0 \le y \le \sin x$ [5]
 - b) Using Gauss-divergence theorem, prove that

$$\iint_{S} (\phi \nabla \Psi - \Psi \nabla \phi) \cdot d\overline{s} = \iiint_{V} (\phi \nabla^{2} \Psi - \Psi \nabla^{2} \phi) dV$$
 [5]

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- Using Stoke's theorem, evaluate: $\int_{C} [3(x-y)dx + 2xzdy + xydz]$
 - Where C is the curve of intersection of paraboloid $x^2 + y^2 = 2z$ and the plane z = 2

[5]

OR

- Q7) a) Evaluate $\int_C \overline{F} \cdot d\overline{r}$, $\overline{F} = (2x + y^2)\overline{i} + (3y 4x)\overline{j}$ where C is the parabolic are $y = x^2$ joining (0, 0) & (1, 1) [5]
 - b) Using Gauss-Divergence Theorem, evaluate $\iint_S \overline{F} \cdot \hat{n} ds$ for $\overline{F} = 4xz\overline{t} y^2\overline{j} + yz\overline{k}$ where S is the surface of the cube bounded by the planes x = 0, x = 2, y = 0, y = 2, z = 0, z = 2 [5]
 - c) Evaluate $\iint_{S} (\nabla \times \overline{F}) \cdot d\overline{s}$ for $\overline{F} = y\overline{i} + z\overline{j} + x\overline{k}$ where S is the surface of the paraboloid $z = 1 x^2 y^2$, $z \ge 0$ [5]
- Q8) a) If $u = x^4 6x^2y^2 + y^4$, find V such that f(z) = u + iv is analytic function. Express f(z) in terms of z. [5]
 - b) Use Cauchy's integral formula to evaluate $\oint_C \frac{e^z}{z+2} dz$ where C is the circle |z+2|=2 [5]
 - Find the bilinear transformation which maps the points 0, -1, i of the z-plane onto the points $2, \infty, \frac{1}{2}(5+i)$ of the W-plane.
- (Q9) a) Show that analytic function f(z) with constant amplitude is constant. [5]
 - b) Apply residue theorem to evaluate $\oint_C \frac{4z^2 + z}{z^2 1} dz$ where C is the contour

$$|z-|=\frac{1}{2}$$
 [5]

Show that the transformation $W = z + \frac{1}{z} 2i$ maps the circle |z| = 2 into an ellipse. Find centre, semi-major and semi-minor axes of ellipse. [5]

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