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SEAT No. :

PA-4

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[5931]-6

S.E. (Electronics / E & TC / Electronics & Computer)

ENGINEERING MATHEMATICS - III

(2019 Pattern) (Semester - I) (207005)

Time : 1 Hour]

[Max. Marks : 30

Instructions to the candidates :

- 1) Answer Q.1 or Q.2 and Q.3 or Q.4.
- 2) Figures to the right indicate full marks.
- 3) Neat diagrams must be drawn wherever necessary.
- 4) Use of non-programmable scientific calculator is allowed.
- 5) Assume suitable data, if necessary.

Q1) a) Solve any two :

[10]

- i) $(D^2 - 4D + 3)y = x^3 e^{2x}$
- ii) Solve by variation of parameters method
 $(D^2 + 4)y = \sec 2x$
- iii) $x^2 \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} - 4y = x^2$

b) Solve : $\frac{dx}{y+zx} = \frac{dy}{-x-yz} = \frac{dz}{x^2-y^2}$

[5]

OR

Q2) a) Solve any two :

[10]

i) $\frac{d^2 y}{dx^2} + 4y = x \sin x$

ii) $(D^2 - 6D + 9)y = \frac{e^{3x}}{x^2}$

Solve by variation of parameters method.

iii) $(x+a)^2 \frac{d^2 y}{dx^2} - 4(x+a) \frac{dy}{dx} + 6y = x$

P.T.O.

- b) A circuit consists of an inductance L and condenser of capacity C in series. An alternating emf $E \sin nt$ is applied to it at time $t = 0$, the initial current and charge being zero, find the current flowing in the circuit at any time t for $w \neq n$ where $w^2 = \frac{1}{LC}$ [5]

Q3) a) Find the Fourier cosine transform of the function $f(x) = \begin{cases} \cos x & 0 < x < a \\ 0 & x > a \end{cases}$ [5]

- b) Attempt any ONE : [5]

i) Find the z -transform of $f(k) = \sin\left(\frac{k\pi}{4} + \frac{\pi}{8}\right), k \geq 0$

- ii) Find the inverse z -transform of

$$f(z) = \frac{1}{\left(z - \frac{1}{2}\right)\left(z - \frac{1}{3}\right)}, |z| > \frac{1}{2}$$

- c) Solve the following difference equation [5]

$$12f(k+2) - 7f(k+1) + f(k) = 0; k \geq 0$$

$$f(0) = 0, f(1) = 3$$

OR

- Q4) a) Attempt any ONE : [5]

i) Find the z -transform of $f(k) = k 5^k, k \geq 0$

- ii) Find inverse z -transform by inversion integral method

$$f(z) = \frac{1}{(z-2)(z-3)}$$

b) Find the Fourier sine transform of [5]

$$f(x) = \begin{cases} x & 0 \leq x \leq 1 \\ 2-x & 1 \leq x \leq 2 \\ 0 & x > 2 \end{cases}$$

c) Solve the following integral equation [5]

$$\int_0^{\infty} f(x) \cos \lambda x dx = e^{-\lambda}, \lambda > 0$$

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