

Total No. of Questions : 8]

SEAT No. :

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[6180]-46A

T.E. (Computer Engineering)

THEORY OF COMPUTATION

(2019 Pattern) (Semester - I) (310242)

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates :

- 1) Answer Q1 or Q2, Q3 or Q4, Q5 or Q6, Q7 or Q8.
- 2) Neat diagrams must be drawn wherever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Assume suitable data, if necessary.

Q1) a) Check whether the string 10010 is a member of the language generated by following grammar by using Cocke-Younger-Kasami Algorithm- [9]

$S \rightarrow AB|BC$

$A \rightarrow BA|0$

$B \rightarrow CC|1$

$C \rightarrow AB|0$

b) Obtain grammar to generate the following language : [8]

$L = \{w : n_a(w) \bmod 2 = 0 \text{ where } w \in \{a, b\}^*\}$

i.e. Language of a and b in which number of number of a's in the string is either zero or in multiple of 2 only.

OR

Q2) a) [9]

$S \rightarrow aB|bA$

$A \rightarrow a|aS|bAA$

$B \rightarrow b|bS|aBB$

Derive using Leftmost Derivation and Rightmost Derivation:

i) bbaaba ii) aaabbb.

Draw parse tree for the same.

P.T.O.

- b) Find context Free Grammar generating each of these languages. [8]
- i) $L_1 = \{a^i b^j c^k \text{ such that } i = j+k \text{ where } i, j, k \geq 1\}$
- ii) $L_2 = \{a^i b^j c^k \text{ such that } j = i+k \text{ where } i, j, k \geq 1\}$

Q3) a) Construct a PDA equivalent to following CFG [10]

i)

$$X \rightarrow 0$$

$$X \rightarrow 0X$$

$$X \rightarrow 1XX$$

$$X \rightarrow XX1$$

$$X \rightarrow X1X$$

ii) $S \rightarrow BD|BC$

$$D \rightarrow SC$$

$$C \rightarrow AA$$

$$B \rightarrow 0$$

$$A \rightarrow 1$$

b) Design a PDA for a language $L = \{a^n b^{2n} | n \geq 1\}$ [8]

OR

Q4) a) Construct a PDA accepting the language $L = \{a^n b^m a^n | n, m \geq 0\}$ by null store. [6]

b) Design a PDA for a language $L = \{XcX^r | X \in \{a,b\}^*$ and string X^r is the reverse of string $X\}$. [6]

c) Obtain a PDA to accept the language -

$$L = \{w | w \in \Sigma^*, \Sigma = \{a,b\} \text{ and } n_a(w) = n_b(w)\} \text{ by final state} [6]$$

Q5) a) Design a Turing machine for well formed parenthesis. [6]

b) Design a TM that accepts all strings over $\{1,0\}$ with even number of 0's and even number of 1's. [8]

c) Construct TM that recognizes language over alphabet 0,1 such that string ends in 10. [4]

OR

- Q6)** a) Construct a TM to accept the language over $\{0,1\}$ containing the substring 001. [6]
 b) Design a TM to multiply a unary number by 2. [8]
 c) Design Turing Machine for 1's Complement. [4]
- Q7)** a) What is post correspondence problem? Explain PCP with following instance of the set of the strings A and B. [8]

	A	B
1.	1	111
2.	10111	10
3.	10	0

- b) State and explain with suitable example [9]
 i) Decidable Problem
 ii) Undecidable Problem
 iii) Church-Turing Thesis.

OR

- Q8)** a) What is reducibility in Computability Theory ? Explain in detail, the polynomial - time reduction approach for proving that a problem is NP-Complete. [8]
 b) Explain with suitable example and diagrams [9]
 i) Halting problem of TM
 ii) Multitape TM
 iii) Universal TM

