

Total No. of Questions : 4]

SEAT No. :

PC399

[6359]-519

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**S.E. (Computer Engineering) (Computer Science & Design Engg.)/  
(Artificial Intelligence & Data Science Engg.)/**

**(Computer Science) (Insem)**

**DISCRETE MATHEMATICS**

**(2019 Pattern) (Semester- III) (210241)**

*Time : 1 Hour]*

*[Max. Marks : 30*

*Instructions to the candidates:*

- 1) *Answer the question of 1 or 2, 3 or 4.*
- 2) *Neat diagrams must be drawn wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Assume suitable data, if necessary.*

**Q1) a)** By using mathematical induction show that  $1+4+7+\dots+(3n-2)=n(3n-1)/2$  for all natural number values of  $n$ . **[5]**

**b)** Explain following terms with example **[5]**

- i) Symmetric difference between set
- ii) Union of set
- iii) Intersection of set
- iv) Subset of a set
- v) Power of the set

**c)** In the survey of 60 people, it was found that 25 read Newsweek magazine, 26 read time, 26 read Fortune. Also 9 read both Newsweek and Fortune, 11 read both Newsweek and Time, 8 read both Time and Fortune and 8 read no magazine at all. **[5]**

- i) Find out the total number of people who read all the three magazines
- ii) Fill in the correct number in all the regions of the Venn diagram
- iii) Determine the number of people who read exactly one magazine

OR

**Q2) a)** Express the contrapositive, converse and inverse form of conditional statement given below:

“If  $x$  is rational, then  $x$  is real”

**[5]**

**P.T.O.**

- b) Let  $p$  be "Mark is Rich" and  $q$  be "Mark is happy" write each of following in symbolic form [5]
- Mark is poor but happy
  - Mark is neither rich nor happy
  - Mark is either rich or happy
  - Mark is Rich and not happy
- c) Explain terms Tautology and Contradiction in truth table with an example [5]

- Q3)** a) Let  $f(x)=x+2$ ,  $g(x)=x-2$ ,  $h(x)=3x$  find  $\text{gof}$ ,  $\text{fog}$ ,  $\text{fof}$ ,  $\text{gog}$ ,  $\text{foh}$ . [5]
- b) For each of these relations on Set  $A=\{1,2,3,4\}$  decide whether it is reflexive, symmetric, transitive or anti-symmetric (one relation may satisfy more than one properties) [5]
- $R_1=\{(1,1), (2,2), (3,3), (4,4)\}$
- $R_2=\{(1,1), (1,2), (2,2), (2,1), (3,3), (4,4)\}$
- $R_3=\{(1,3), (1,4), (2,3), (2,4), (3,1), (3,4)\}$
- c) Draw a hasse diagram for  $(S, \leq)$  where  $S=\{1,2,3,4,5,6\}$   $\leq$  is defined as  $a \leq b$  if  $a$  divides  $b$ , i.e.  $b$  is an integer multiple of  $a$ . [5]

OR

- Q4)** a) Let  $A=\{1,2,3,4\}$  and  $R=\{(1,2), (2,1), (2,3), (3,4)\}$  Find transitive closure of relation  $R$  using Warshall's algorithm. [5]
- b) What is Equivalence relation? Explain properties of binary relations. [5]
- c) Explain the various types of functions. [5]

